
Hopf25

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Nichols Algebras versus Bimodule Connections

One of the well-known motivations for Nichols algebras comes from the noncommutative geometry of quantum groups, and in particular the Woronowicz construction of Nichols algebras from bicovariant differential calculi. In recent years, a quantum principal bundle variation on the Woronowicz construction was discovered, and applied to the quantum Grassmannians' Heckenberger-Kolb calculi. Moreover, it was also conjectured that this construction extends to the B,C, and D series irreducible quantum flag manifolds. In this talk we show that this conjecture is false, explaining why, for the B₂ and C₃ cases, no equivariant Nichols algebra description exists. However, we produce an alternative description of these quantum exterior algebras in terms of the bimodule map of Levi-Civita connections of the Heckenberger-Kolb calculi. Time permitting, possible extensions of this work to the Lusztig calculi of the full quantum flag manifolds will be discussed.